

Asteroseismology of ZZ Ceti stars with fully evolutionary white dwarf models

I. The impact of the uncertainties from prior evolution on the period spectrum

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ABSTRACT

Context. ZZ Ceti stars are pulsating white dwarfs with a carbon-oxygen core build up during the core helium burning and thermally pulsing Asymptotic Giant Branch phases. Through the interpretation of their pulsation periods by means of asteroseismology, details about their origin and evolution can be inferred. The whole pulsation spectrum exhibited by ZZ Ceti stars strongly depends on the inner chemical structure. At present, there are several processes affecting the chemical profiles that are still not accurately determined. **Aims.** We present a study of the impact of the current uncertainties of the white dwarf formation and evolution on the expected pulsation properties of ZZ Ceti stars.

Methods. Our analysis is based on a set of carbon-oxygen core white dwarf models with masses 0.548 and 0.837 M_{\odot} derived from full evolutionary computations from the ZAMS to the ZZ Ceti domain. We have considered models in which we varied the number of thermal pulses, the amount of overshooting, and the $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ reaction rate within their uncertainties.

Results. We explore the impact of these major uncertainties in prior evolution on the chemical structure and the expected pulsation spectrum. We find that these uncertainties yield significant changes in the g-mode pulsation periods.

Conclusions. We conclude that the uncertainties in the white dwarf progenitor evolution should be taken into account in detailed asteroseismological analysis of these pulsating stars.

Key words. asteroseismology — stars: oscillations — white dwarfs — stars: evolution — stars: interiors

1. Introduction

White dwarf (WD) stars are the final result of the evolution of low- and intermediate-mass (up to $\sim 10.6 M_{\odot}$, Woosley & Heger 2015) stars. A carbon-oxygen core composition is expected in most of WDs, which is the result of He burning in the core of progenitor stars. The exact proportions of the resulting carbon-oxygen composition is a key factor that determines the cooling properties of the emerging WDs. In addition, the precise shape of the chemical abundance distribution is critical for the pulsational properties of these stars.

ZZ Ceti (or DAV) variable stars are pulsating WDs with H-rich atmospheres. Located in a narrow instability strip with effective temperatures between 10500 K and 12500 K (Fontaine & Brassard 2008; Winget & Kepler 2008; Althaus et al. 2010b), they constitute the most numerous class of compact pulsators. These stars are characterized by multimode photometric variations caused by non-radial g-mode pulsations of low degree ($\ell \leq 2$) with periods between 70 and 1500 s and amplitudes up to 0.30 mag. These pulsations are thought to be excited by both the $\kappa - \gamma$ mechanism acting on the base of the H partial ionization zone (Dolez & Vauclair 1981; Winget et al. 1982) and the “convective driving” mechanism (Brickhill 1991; Goldreich & Wu 1999; Saio 2013). Since the discovery of the

first ZZ Ceti star, HL Tau 76 by Landolt (1968), a continuous effort has been made to model the interior of these variable stars.

The comparison of the observed pulsation periods in WD with the periods computed from appropriate theoretical representative models allows us to infer details about the origin and evolution of the progenitor star (Fontaine & Brassard 2008; Winget & Kepler 2008; Althaus et al. 2010b). In particular, asteroseismological analysis of ZZ Ceti stars provides strong constraints on the stellar mass, the thickness of the outer envelopes, the core chemical composition, and the stellar rotation rates (e.g., Romero et al. 2012). In addition, ZZ Ceti asteroseismology is a valuable tool for studying axions (Isern et al. 1992, 2010; Bischoff-Kim et al. 2008; Córscico et al. 2012, 2016) and crystallization (Montgomery et al. 1999; Córscico et al. 2004, 2005; Metcalfe et al. 2004; Kanaan et al. 2005; Romero et al. 2013).

There are two main approaches adopted for WD asteroseismology. The first one employs static stellar models with parametrized chemical profiles. This approach has the advantage that it allows a full exploration of the parameter space to find an optimal seismic model (Bischoff-Kim & Østensen 2011; Bischoff-Kim et al. 2014; Giammichele et al. 2014, 2016). The other approach uses fully evolutionary models resulting from the complete evolution of the progenitor star, from the Zero Age Main Sequence (ZAMS) to the WD stage (Romero et al. 2012,

2013). This approach involves the most detailed and updated input physics, in particular regarding the internal chemical structure, a crucial aspect for correctly disentangle the information encoded in the pulsation patterns of variable WDs. This method has been successfully applied in different classes of pulsating WDs (see Romero et al. 2012, 2013, in the case of ZZ Ceti stars). However, asteroseismological inferences based on this approach do not take into account the current uncertainties neither in the modeling nor in the input physics of WD progenitors. An assessment of the impact of these uncertainties on the pulsation periods of ZZ Ceti stars, constitutes the core feature of the present paper.

In this regard, there exist several important uncertainties linked to WD prior evolution that should be explored. As well known, the exact proportions of the carbon-oxygen composition of the WD core constitute a key factor that strongly impact the cooling properties of the emerging WDs. In addition, the precise shape of the chemical abundance distribution is critical for the pulsational properties of WDs. The main uncertainty affecting the carbon-oxygen chemical profiles and the cooling times in WDs is related with the $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ reaction rate. Salaris et al. (2010) studied the differences found in cooling times that arise from uncertainties in several processes during the pre-WD evolution, and found that the changes in cooling times associated with the $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ reaction rate was of about 7%. More recently, Fields et al. (2016) have carried out an extensive study of the impact of uncertainties in several reaction rates during core H and He burning on important stellar parameters as mass, age, carbon-oxygen central abundances and central density. They found that uncertainties in the $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ and $^{14}\text{N}(p, \gamma)^{15}\text{O}$ are dominant. Another uncertain process that modifies the chemical structure is overshooting (OV). The precise size of the convective core and the mixing regions are currently one of the major uncertainties affecting the computations of stellar structure and evolution. In particular, the amount of OV considered during core He burning is not completely known and strongly modifies the internal carbon-oxygen profile, the mass of the convective core and the temperature stratification. Current uncertainties in physical processes operative during the thermally pulsing Asymptotic Giant Branch (TP-AGB) phase also leave their signature in the final chemical abundance distribution expected in WDs. In particular, the outermost-layer chemical stratification of the WD core is built up during the TP-AGB phase and depends strongly on the occurrence of OV and mass loss during this stage. In particular, the mass of the intershell rich in He and C that is left by the short-lived He flash convective zone depends on both the amount of OV and the number of thermal pulses (TP) which is determined by the poorly constrained efficiency of mass loss (Karakas & Lattanzio 2014).

In this paper, we will assess the impact of the main uncertain processes in the evolutionary history of the progenitors on the chemical profiles and the pulsation period spectrum of ZZ Ceti stars. In particular, we focus on the effects of OV during the core He burning stage, the occurrence and number of TP in the AGB phase, and the uncertainties in the $^{12}\text{C}+\alpha$ reaction rate. To this end, we computed evolutionary sequences from the ZAMS, through the TP-AGB stage following the evolution of the remnant star to the WD state until the domain of the ZZ Ceti instability strip. The sequences are characterized by progenitor masses of 1.5 and $4M_{\odot}$ with initial metallicity of $Z = 0.01$.

This paper is organized as follow: in Sect. 2 we introduce the numerical tools employed and the input physics assumed in the evolutionary calculations, and the pulsation code employed. In Sect.3 we present our results. Finally, in Sect. 4 we conclude the paper by summarizing our findings.

2. Computational tools

2.1. Evolutionary code and input physics

The DA WD evolutionary models calculated in this work were generated with the LPCODE evolutionary code, which produces detailed WD models based on updated physical description (Althaus et al. 2005, 2010a; Renedo et al. 2010; Romero et al. 2012; Miller Bertolami 2016). LPCODE has been employed to study different aspects of the evolution of low-mass stars (Wachlin et al. 2011; Althaus et al. 2013, 2015), formation of Horizontal Branch stars Miller Bertolami et al. (2008), Extremely Low Mass WDs (Althaus et al. 2013), AGB and post-AGB evolution (Miller Bertolami 2016). We detail below the main physical ingredients of LPCODE relevant to this work:

- standard mixing-length theory with the free parameter $\alpha = 1.61$ was adopted for pre-WD stages;
- diffusive OV during the evolutionary stages prior to the TP-AGB phase, were allowed to occur following the description of Herwig et al. (1997). We adopted $f = 0.016$ for all sequences, except when indicated. OV is relevant for the final chemical stratification of the WD (Prada Moroni & Straniero 2002; Straniero et al. 2003);
- breathing pulses at the end of core He burning effect, which occur at the end of core He burning, were suppressed (see Straniero et al. (2003) for a discussion on this topic);
- LPCODE considers a simultaneous treatment of non-instantaneous mixing and burning of elements. Our nuclear network accounts explicitly for the following 16 elements: ^1H , ^2H , ^3He , ^4He , ^7Li , ^7Be , ^{12}C , ^{13}C , ^{14}N , ^{15}N , ^{16}O , ^{17}O , ^{18}O , ^{19}F , ^{20}Ne , ^{22}Ne and 34 thermonuclear reaction rates (Althaus et al. 2005);
- gravitational settling, and thermal and chemical diffusion was taken into account for ^1H , ^3He , ^4He , ^{12}C , ^{13}C , ^{14}N , ^{16}O (Althaus et al. 2003);
- during WD phase, chemical rehomogenization of the inner carbon-oxygen profile induced by Rayleigh-Taylor (RT) instabilities was implemented following Salaris et al. (1997);
- for the high-density regime characteristic of WDs, we used the equation of state of Segretain et al. (1994), which accounts for all the important contributions for both the liquid and solid phases.

We computed the evolution of our sequences throughout all the evolutionary stages of the WD progenitor, including the stable core He burning and the TP-AGB and post-AGB phases. We want to mention that LPCODE has been compared against other WD evolution code showing that the differences in the WDs cooling times that comes from the different numerical implementations of the stellar evolution equations were by 2% Salaris et al. (2013).

2.2. Pulsation code

For the pulsation analysis presented in this work we employed the LP-PUL adiabatic non-radial pulsation code described in Córscico & Althaus (2006), coupled to the LPCODE evolutionary code. LP-PUL solves the full fourth-order set of real equations and boundary conditions governing linear, adiabatic and non-radial stellar pulsations. The pulsation code provides the eigenfrequency $\omega_{\ell,k}$ —where k is the radial order of the mode—and the dimensionless eigenfunctions y_1, \dots, y_4 . LP-PUL computes the periods ($\Pi_{\ell,k}$), rotation splitting coefficients ($C_{\ell,k}$), oscillation kinetic energy ($K_{\ell,k}$) and weight functions ($W_{\ell,k}$). The expressions to compute these quantities can be found in the Appendix

of Córscico & Althaus (2006). The Brunt-Väisälä frequency (N) is computed as (Tassoul et al. 1990):

$$N^2 = \frac{g^2 \rho}{P} \frac{\chi_T}{\chi_P} (\nabla_{\text{ad}} - \nabla + B), \quad (1)$$

where

$$B = -\frac{1}{\chi_T} \sum_{i=1}^{n-1} \chi_{X_i} \frac{d \ln X_i}{d \ln \rho}, \quad (2)$$

is the Ledoux term and contains the contribution coming from the chemical composition changes, and

$$\chi_T = \left[\frac{\partial \ln P}{\partial T} \right]_{\rho}, \quad \chi_P = \left[\frac{\partial \ln P}{\partial \rho} \right]_T, \quad \chi_{X_i} = \left[\frac{\partial \ln P}{\partial X_i} \right]_{\rho, T, X_{j \neq i}}. \quad (3)$$

3. Pulsational analysis

In this section we study the uncertainties during the prior evolution of the progenitor star that affects the chemical structure of the emerging WDs and their pulsation period spectra. In particular, we explore:

1. The occurrence of TP during the AGB phase of the progenitor star.
2. The occurrence of OV during core He burning.
3. The $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ reaction rate.

We concentrate on template models characterized by $M_{\star} = 0.548, 0.837 M_{\odot}$, with H envelope mass of $M_{\text{H}} \sim 4 \times 10^{-6} M_{\star}$ at $T_{\text{eff}} \sim 12\,000\text{ K}$, and considered the pulsation period spectrum for modes with $\ell = 1$.

In Fig. 1 we show the internal chemical profiles and the logarithm squared Brunt-Väisälä frequency in terms of the outer mass fraction for both models at the ZZ Ceti domain. Our models are characterized by three chemical transition regions from center to the surface: a chemical interface of C and O, a double-layered chemical structure involving He, C and O, and an interface of He/H. The existence of these three transition zones induces “bumps” in the shape of the Brunt-Väisälä frequency which strongly affects the whole structure of the pulsation spectrum of the star, in particular the mode-trapping properties (Brassard et al. 1992; Bradley 1996; Córscico et al. 2002). These features play a crucial role acting as “filters” by trapping the mode oscillation energy close to the surface, or confining it in the core.

Next, we compare the pulsation properties of the models considered for each case. Since the models compared have the same stellar mass¹, effective temperature and mass of the H envelope, the differences found in the pulsation properties are strictly due to the differences in the chemical structure resulting from different kinds of the progenitor evolution.

3.1. Occurrence of TP in AGB

In this section we explore the impact on the chemical profiles when the progenitor evolves through the TP-AGB phase. Because during this phase a pulse-driven convection zone develops,

the building of an intershell region and a double-layered chemical structure is expected at the bottom of the He buffer. The size of this region decreases with the number of TP, i.e., as the star evolves through the TP-AGB, as consequence of the He-burning shell. The number of TP experienced by the progenitor star is uncertain and depends on the rate at which mass is lost during the TP-AGB phase, on the initial metallicity of progenitor star, as well as, to a less extent, on the occurrence of extra-mixing in the pulse-driven convection zone (Herwig 2000). To quantify the impact of all these uncertainties on the pulsational properties of ZZ Ceti stars, we have explored the situation in which the progenitor experiences 3 and 10 TP (hereinafter referenced as 3TP and 10 TP models) by forcing the departure from the TP-AGB phase at specific stages. In addition, we have considered the extreme situation in which the star is forced to abandon the AGB phase before the occurrence of the first TP (hereinafter referred to as 0TP model).

In Fig. 1 we display the chemical profiles (upper panel) for the most abundant elements, and the logarithm of the squared Brunt-Väisälä (B-V) frequency (lower panel) in terms of the outer mass. As mentioned, the evolution through the TP-AGB leaves its signature on the chemical profile of our models with the formation of an intershell region rich in He and C at the bottom of the He buffer. The presence of C in the intershell region stems from the short lived convective mixing that has driven the C-rich zone upward during the peak of the He pulse on the AGB (Althaus et al. 2010a). As we mentioned, the size of this intershell region depends on the number of TP experienced by the star, decreasing as the number of TP increases (see later in this Section). For the low-mass models, we find that this intershell region formed at the TP-AGB is expected to survive when the stars reach the ZZ Ceti phase. On the other hand, for more massive stars we do not expect this region to be present at the ZZ Ceti stage. This is due that the diffusion processes acting during the WD cooling phase are more efficient for massive stars, thus completely eroding it (Althaus et al. 2010a). We note that the impact on the chemical structure, and in consequence, on the B-V frequency, is more pronounced for the less massive model (see lower panels of Fig. 1). The results for the 0TP model are shown with dashed red lines in the upper panels of Fig. 1. Note that in this case, no intershell region is expected. In the case of the 10 TP model sequence, the intershell region becomes less massive, and it is removed by diffusion by the time the ZZ Ceti stage is reached more easily than in the case of the 3TP model. This is borne out by Fig. 2 which depicts the He abundance distribution below the envelope of the emerging WD.

The impact of considering different number of TP on the period spectrum of the models, can be seen in Fig. 3. In this plot, we show the resulting period differences ($\Delta P_k \equiv P_{k,0\text{TP}} - P_{k,3\text{TP}}$) between the 0TP and 3TP models (solid line, filled circles) and the period differences ($\Delta P_k \equiv P_{k,10\text{TP}} - P_{k,3\text{TP}}$) between the 10TP and 3TP models (dashed line, empty circles) as a function of the radial order k . We found that the resulting changes in the periods (at fixed k) are more pronounced in the case of the less massive model. These substantial variations —high as 22 s— are not solely due to the intershell region (or the overall shape of the profile), but also due to the shift outward of the core/He main chemical transition region.

Not surprisingly, the expectation for the massive model are markedly different. Indeed, in this case the period differences are on average between 2 and 3 s, with some modes reaching period differences as high as ~ 8 s. These smaller changes resulting in the case of the massive model are due to the slight differences

¹ We rescaled the stellar mass when necessary.

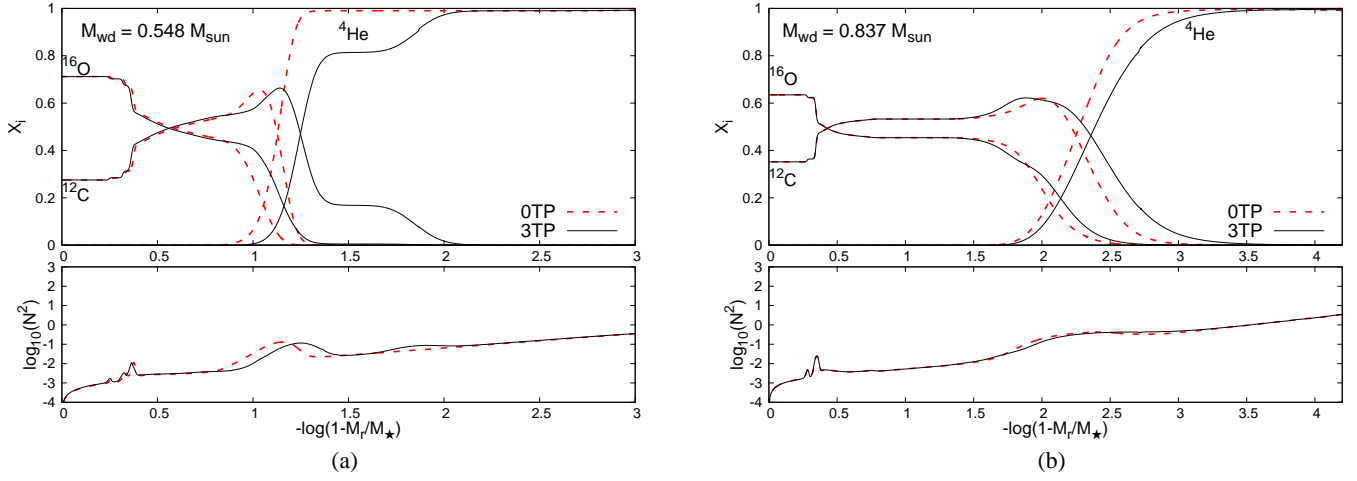


Fig. 1. Upper panels: inner O, C and He abundance distribution in terms of the outer mass fraction for the two stellar models considered in our analysis at $T_{\text{eff}} \sim 12\,000$ K. 0TP refers to the expected chemical profiles resulting from a progenitor before the occurrence of the first TP (red dashed line). 3TP corresponds to the case of the chemical profiles resulting from a progenitor at end of the third TP (black solid line).

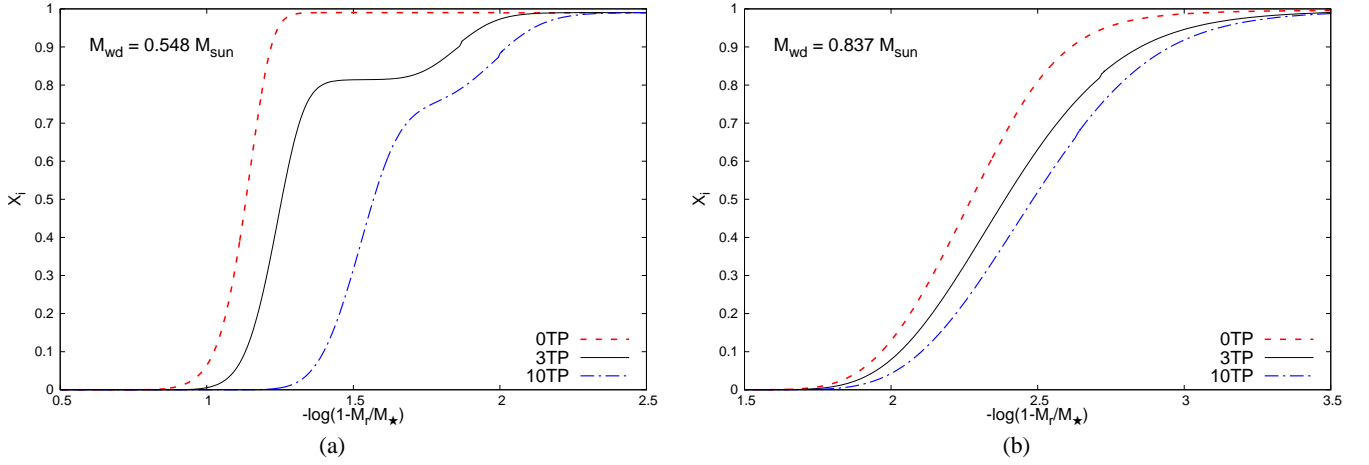


Fig. 2. Inner He abundance distribution in terms of the outer mass for models at the ZZ Ceti stage for which the progenitor experienced no TP (0TP), three TP (3TP), and ten TP (10TP) models. The intershell region is eroded completely for the massive model.

found in chemical profiles. In fact, no intershell is expected to occur at the ZZ Ceti domain.

3.2. Occurrence of OV during core He burning

The occurrence of extra mixing episodes during core He burning strongly affects the final shape of the carbon-oxygen core. To quantify the impact of the presence of core OV on the period spectrum of ZZ Ceti stars, we have considered the extreme situation in which no OV is allowed during the core He burning (3TP-NOV model), and compared it to the template 3TP model, which, as we mentioned, takes into account OV during core He burning.

We start by examining Fig. 4 that shows the inner chemical profiles at the ZZ Ceti stage. Note that models with OV are characterized by lower central C abundances. This is because the ingestion of fresh He in a C-rich zone favours the consumption of C via the reaction $^{12}\text{C} + \alpha$, with the consequent increase of ^{16}O . It is worth noting that this change in the central value of C and O does not modify the B-V frequency (lower panel). However, the B-V frequency is notoriously affected by the steep variation in the carbon-oxygen profile at $-\log(1 - M_r/M_*) \sim 0.4$ left by

core OV. The resulting differences in the value of the periods are shown in Fig. 5. We find that OV introduces absolute differences of 2 to 4 s on average, markedly lower than the period differences resulting from uncertainties in the TP-AGB phase. Note also that the average of the period differences resulting from OV are similar for both stellar masses.

3.3. Uncertainties in the $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ reaction rate

To determine the impact of the uncertainties in the $^{12}\text{C} + \alpha$ reaction rate, we computed the core He burning phase of the progenitors by considering three different values for the $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ reaction rate, and followed the evolution until the progenitor experiences several TP in the AGB-TP phase. We considered the reaction rates provided by Angulo et al. (1999) (Nacre, our reference model), and the extreme high and low values from Kunz et al. (2002) (Kh and Kl models, respectively). These high and low values are derived from the uncertainty for the recommended rate listed in that work. The use of these extreme values for this reaction rate allows us to account for the uncertainties in the carbon-oxygen chemical profiles of WD. In Fig. 6 we plot the temperature dependence of the ratio between the Kh and Nacre,

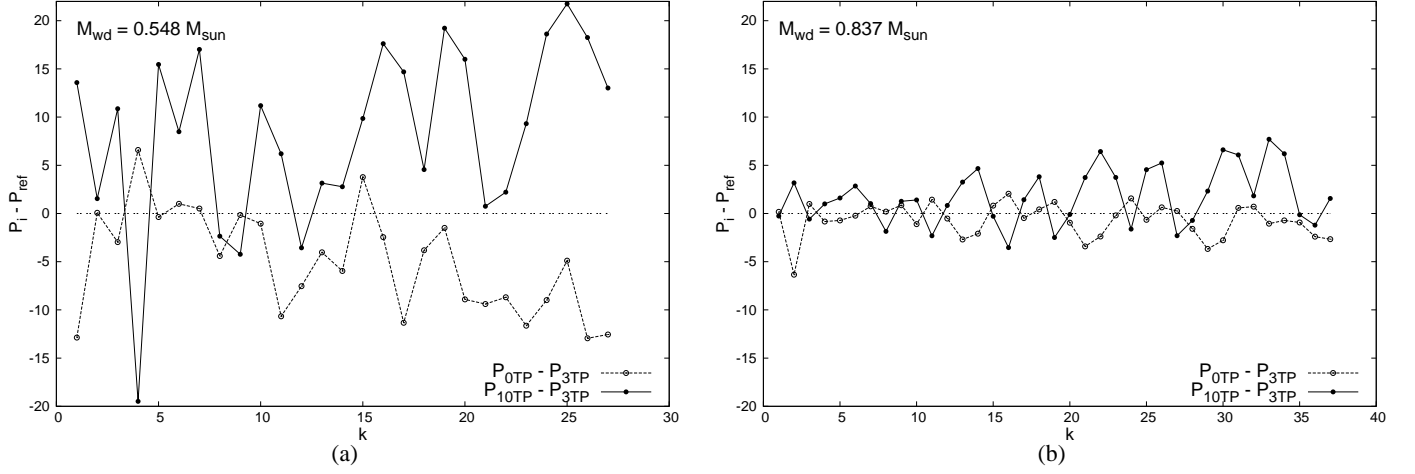


Fig. 3. Period differences (with fixed radial order k) in terms of k between the 0TP and 3TP models (black dashed line) and between the 10TP and 3TP models (black solid line) for the $M_\star = 0.548M_\odot$ and $M_\star = 0.837M_\odot$ WD models (left and right panels, respectively).

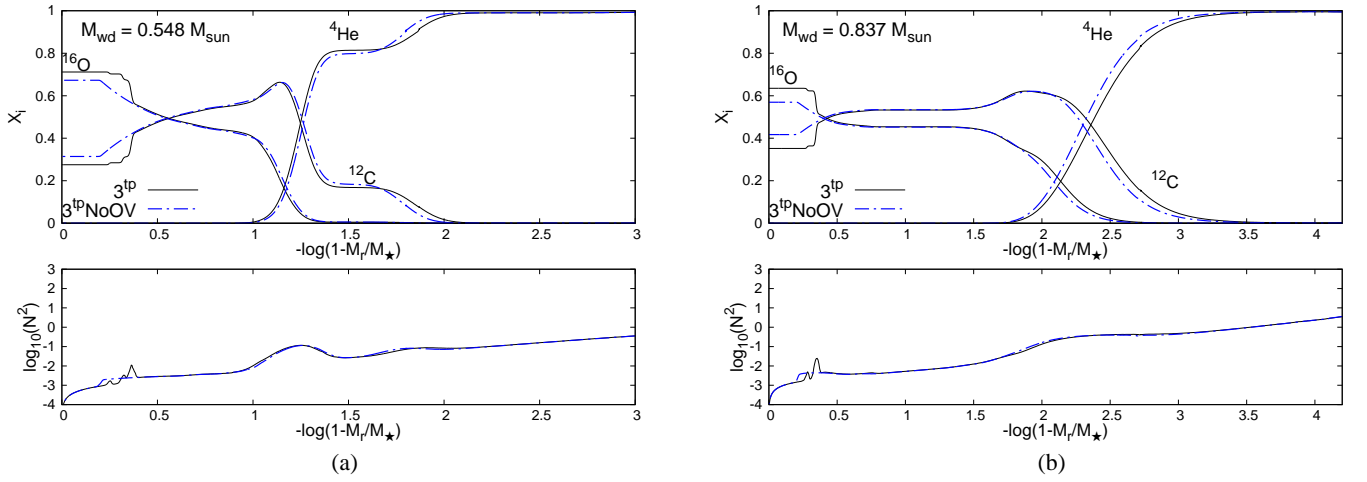


Fig. 4. Same as Fig. 1, but for models at the third TP calculated with an OV parameter $f = 0.016$ (3TP) and with $f = 0$ (3TP-NOV) during core He burning.

and K1 an Nacre reaction rates. Note that for core He burning temperatures ($\sim 2 \times 10^8$ K, grey zone), $\sigma_{\text{Kl}}/\sigma_{\text{Nacre}} \sim 0.55$ and $\sigma_{\text{Kh}}/\sigma_{\text{Nacre}} \sim 1.1$. The impact on the chemical profiles at the ZZ Ceti stage is depicted in Fig. 7. We found differences in the carbon-oxygen abundances, in the location of the O/C and O/C/He chemical transitions, and in the abundances of the intershell region. As expected, the ^{16}O abundance is larger for the models computed with the Kh reaction rate. Models that have been computed assuming the Nacre and Kh reaction rates exhibit quite similar chemical structures. Differences in the B-V frequency are found at the carbon-oxygen and triple transition (see lower panels of Fig. 7).

The resulting impact on the pulsation periods can be seen in Fig. 8, where we plot the differences between the periods predicted by the Kh and Nacre models (dashed line, empty circles) and the differences predicted by the Kl and Nacre models (solid line, filled circles). Low-order modes are, in general, more affected when the Kl reaction rate is assumed. In particular, for the $0.548M_\odot$ model, appreciable differences are expected for both low and high radial-order modes, with maximum differences of $|\Delta P| \sim 11$ s. By contrast, in the case of the massive model, small period differences are found for modes with radial orders $k < 23$ independently of the adopted rate, with a maximum of $|\Delta P| \sim 5$

s. These small variations found in low-order modes reflect the much more smoother behaviour of the chemical profile at the outermost part of the carbon-oxygen core in the case of the massive model. But, for radial orders $k > 23$, appreciable differences are found, reaching $|\Delta P| \sim 18$ s at most. The appreciable differences found for modes with radial orders $k > 23$ stems from the fact that some modes of high radial order k are sensitive to the chemical structure of the core.

4. Summary and conclusions

In this paper, we studied the impact of uncertainties from progenitor evolution on the pulsational properties of ZZ Ceti WD stars. We focused on the occurrence of TP in the AGB stage, the occurrence of OV during the core He burning and also the uncertainties in the $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ reaction rate. Our models were derived from the full and complete evolution from the ZAMS, through the TP-AGB. Evolution of our model sequences was followed to the domain of ZZ Ceti stars, for which we computed the adiabatic g -mode pulsation properties. We computed different sets of models in which we varied the amount of OV during core He burning, the $^{12}\text{C}(\alpha, \gamma)^{16}\text{O}$ reaction rate, and the occurrence and number of TP during the TP-AGB phase.

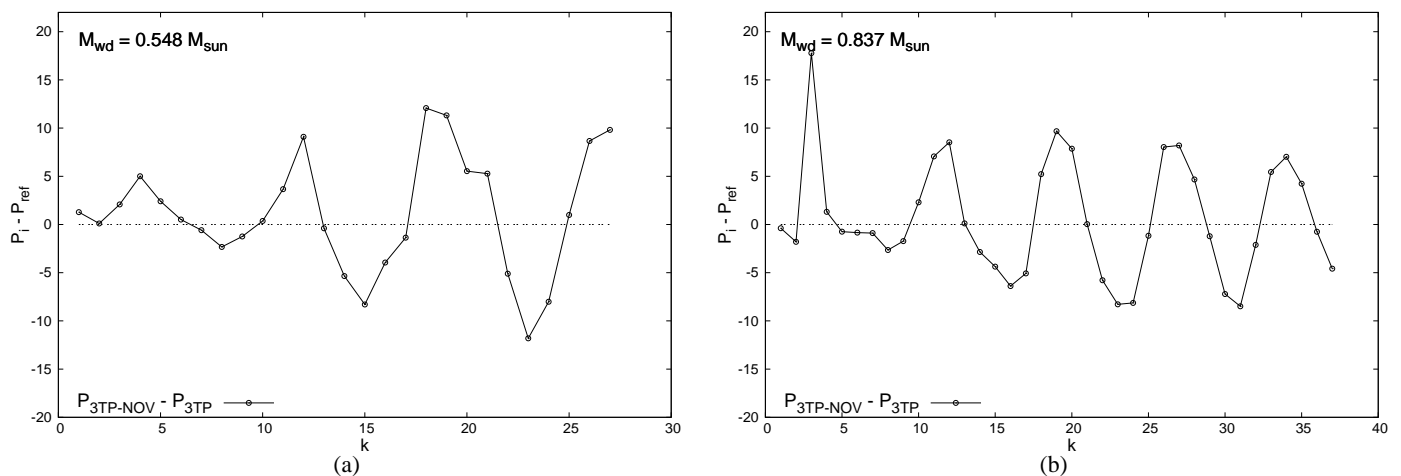


Fig. 5. Same as Fig. 3 but for the 3TP and 3TP-NOV models shown in Fig. 4.

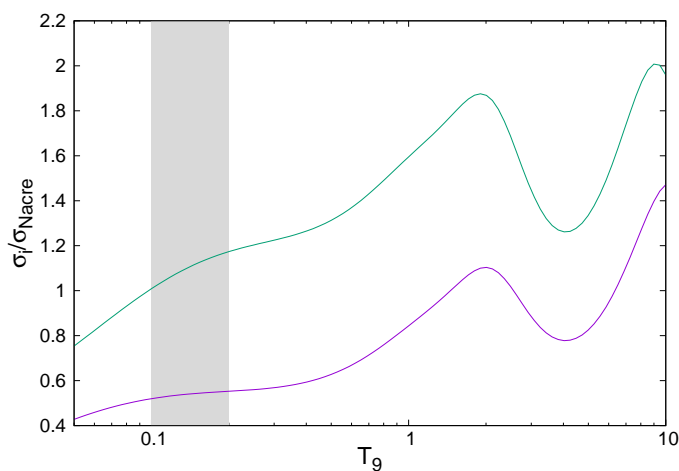


Fig. 6. Ratio between the Kh and Nacre, and Kl and Nacre reaction rates (upper and lower curves, respectively) as a function of temperature. Grey region denotes the typical temperatures expected during the core-He burning.

We have found that if progenitor evolves or not through the TP-AGB phase makes an important point as far as the pulsational properties at the ZZ Ceti stage are concerned. In particular, we found that the resulting changes in the periods (at fixed k) are more pronounced in the case of the less massive model, with period differences on average between 5 and 10 s. However, for massive models, the period differences are markedly smaller ($\sim 2 - 3$ s). This is mainly due to the shift of the core/He main chemical transition is less pronounced and the double layered chemical structure build up during the last TP on the AGB, which impacts the period spectrum of pulsating WDs (Althaus et al. 2010a), is completely eroded by element diffusion in the massive WDs ($M_\star \gtrsim 0.80 M_\odot$) by the time the domain of the ZZ Ceti stars is reached.

On the other hand, the occurrence of OV during the core He burning leaves imprints on the Brunt-Väisälä frequency, resulting in absolute differences of 2 to 4 s on average in the pulsation periods, as compared with the situation in which OV is disregarded. This conclusion is the same regardless the stellar mass.

Finally, uncertainties related with the $^{12}\text{C}+\alpha$ reaction rate affects both O, C, and He abundances and the location of the chem-

ical transitions. In the case of less massive models, the changes in period induced by these different chemical structures amount to, at most, $|\Delta P| \sim 11$ s for some specific modes. For our massive model, period differences are relevant only for $k \geq 20$ modes. We mention that the period differences resulting from uncertainties of the $^{12}\text{C}+\alpha$ reaction rate are less relevant than the period differences inflicted by uncertainties in OV during core He burning and by the occurrence of TP.

We conclude that the current uncertainties in the chemical profiles of WDs, resulting from the progenitor evolution, impact the pulsational period spectrum of ZZ Ceti stars. In this paper, we have quantified for the first time the magnitude of this impact. The amount of the resulting period changes is larger than the typical uncertainties of the observed periods and also higher than the typical accuracy of the period-to-period fits of Romero et al. (2012) which is, on average, less than 3.5 s. However, we stress that the differences of periods we found have to be considered as upper limits, since they correspond to extreme uncertainties in prior evolution. In addition, the largest period differences are found to occur only at certain specific modes, and not at the whole period spectrum. Anyway, these uncertainties should be taken into account in any asteroseismological analysis of ZZ Ceti stars. We defer to a future work an assesment of this issue.

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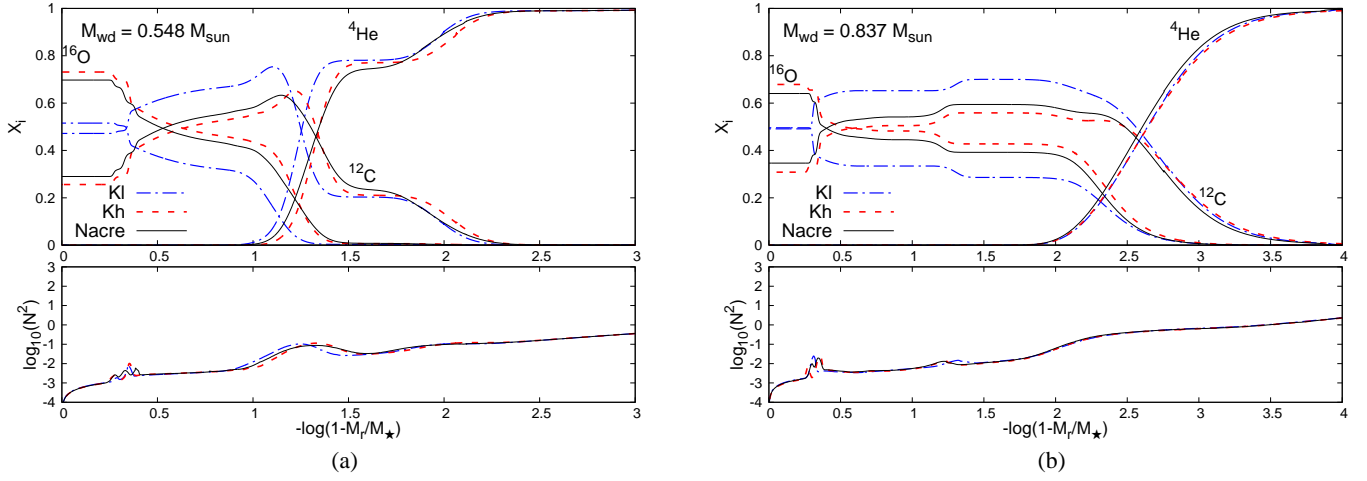


Fig. 7. Same as Fig. 1 but for models computed with three different $^{12}\text{C}+\alpha$ reaction rates: Angulo et al. (1999) (Nacre, black solid line), the higher (KH), and the lower (KL) reaction rates from Kunz et al. (2002) (red dashed line and blue dashed line, respectively).

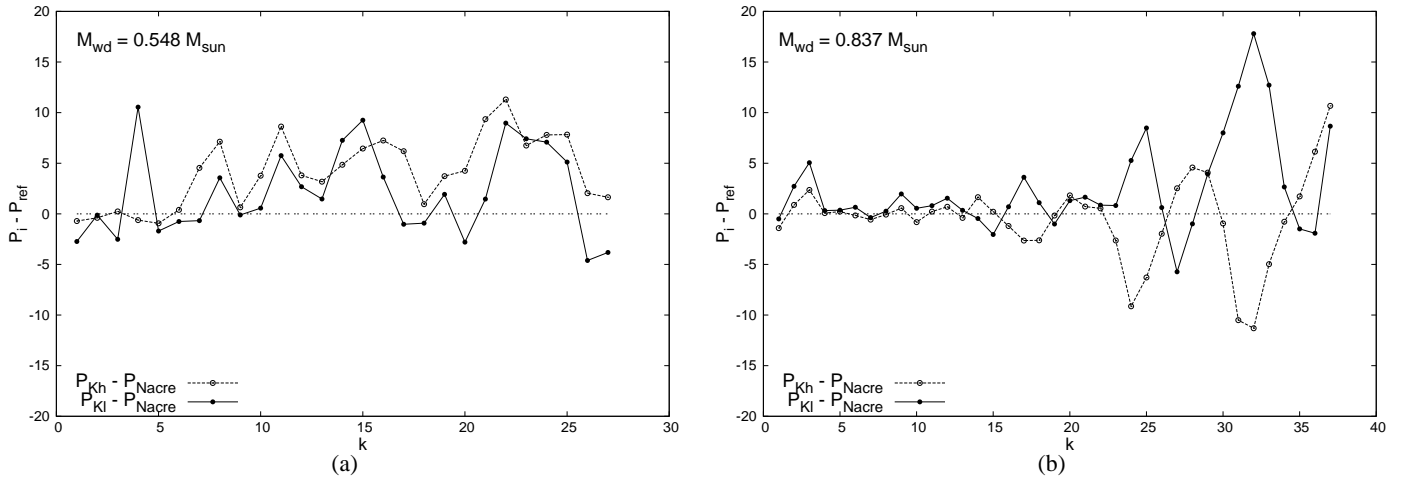


Fig. 8. Same as Fig. 3 but for the period differences between Kh and Nacre models, (black dashed line) and Kl and Nacre models (black solid line).

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